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6489706, A2000-05-4110H-071, B2000-03-5210-074; 20000201.

Title

An efficient algorithm for the RCS modulation prediction from jet inlet-engines.

Author(s)Barka-A; Bobillot-G.**Author affiliation**

ONERA, Chatillon, France.

Source

IEEE Antennas and Propagation Society International Symposium. 1999 Digest, vol.4, Orlando, FL, USA, 11-16 July 1999.

Sponsors: Nat. Sci. Found.

In: p.2566-9 vol.4, 1999.

ISSN

ISBN: 0-7803-5639-X, CCCC: 0 7803 5639 X/99/ (\$10.00).

Publication year

1999.

Language

EN.

Publication type

CPP Conference Paper.

Treatment codes

T Theoretical or Mathematical.

Abstract

The electromagnetic scattering from the interior of a complex jet engine inlet contributes significantly to the overall **radar cross section** (RCS) of a modern jet **aircraft**. Previously we have presented a general multi-domain and multi-method coupling scheme, based on generalized scattering matrices computations of three-dimensional inlet subdomains. This method is really suitable in a context of parametric investigations (local inlet engine modifications). In this paper we discuss a new algorithm providing the **radar** modulation due to a set of rotating blades computed with only one solution for any blade position. A validation of this method is presented on a simplified rotating structure connected with an evolutive inlet. (2 refs).

Descriptors

aerospace engines; aircraft; electromagnetic wave scattering; finite element analysis; integral equations; modulation; radar cross sections; S-matrix theory.

Keywords

efficient algorithm; RCS modulation prediction; jet inlet engines; electromagnetic scattering; **radar cross section**; jet **aircraft**; multi domain coupling scheme; multi method coupling scheme; generalized scattering matrices; three dimensional inlet subdomains; parametric investigations; local inlet engine modifications; algorithm; **radar** modulation; rotating blades; blade position; rotating structure; evolutive inlet; EFIE solver; 3D **finite element** method.

Classification codes

A4110H (Electromagnetic waves: theory).
A0260 (Numerical approximation and **analysis**).
B5210 (Electromagnetic wave propagation).
B0290H (Linear algebra (numerical **analysis**)).
B0290T (**Finite element analysis**).
B0290R (Integral equations (numerical **analysis**)).

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Accession number & update

4484648, A9321-4110H-003, B9311-5210-003; 930916.

Title

A new **finite element** formulation for RF scattering by complex bodies of revolution.

Author(s)

Khebir-A; D-Angelo-J; Joseph-J.

Author affiliation

General Electric Corp Res & Dev, Schenectady, NY, USA.

Source

IEEE-Transactions-on-Antennas-and-Propagation (USA), vol.41, no.5, p.534-41, May 1993.

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IETPAK.

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ISSN: 0018-926X, CCCC: 0018-926X/93/ (\$03.00).

Publication year

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Language

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Publication type

J Journal Paper.

Treatment codes

T Theoretical or Mathematical.

Abstract

A formulation for and results of solving electromagnetic scattering from complex inhomogeneous **axisymmetric** bodies are presented. The approach presented uses the **finite element** method in the frequency domain. A node-based approach is used to solve for the three components of the electric or magnetic field. The **finite element** mesh is truncated using a three-dimensional vector absorbing boundary condition based on the Wilcox expansion theorem. A harmonic expansion of the near-field solution obtained from the **finite element** solution is used to compute the far fields and **radar cross section**. (23 refs).

Descriptors

boundary-value-problems; electromagnetic-wave-scattering; finite-element-analysis; frequency-domain-analysis; radar-cross-sections.

Keywords

electric field; **finite element** formulation; RF scattering; complex bodies of revolution; electromagnetic scattering; inhomogeneous **axisymmetric** bodies; frequency domain; node based approach; magnetic field; **finite element** mesh; three dimensional vector absorbing boundary condition; Wilcox expansion theorem; harmonic expansion; near field solution; far fields; **radar cross section**.

Classification codes

A4110H (Electromagnetic waves: theory).
 A0260 (Numerical approximation and **analysis**).
 B5210 (Electromagnetic wave propagation).
 B0290T (**Finite element analysis**).

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Finite element analysis of axisymmetric radomes

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Abstract:

A two-step technique for the analysis of axisymmetric radomes is presented. axisymmetric finite-element approach is employed, together with an absorbing condition for mesh truncation, to determine the near fields scattered by an er radome illuminated by a distant source. Next, the reciprocity theorem is involved to determine the far-field pattern of an antenna encased by the radome, by comparing the interaction between the current distribution on the antenna and the near-field determined in the first step. The details of the formulation are presented along with numerical results for two different arrays enclosed by radomes of varying per

Index Terms:

antenna accessories antenna arrays antenna radiation patterns boundary-value problem element analysis mesh generation absorbing boundary condition axisymmetric radar distribution far-field pattern finite-element approach mesh truncation numerical results reciprocity theorem scattered near field two-step technique

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Finite Element Analysis of Axisymmetric Radomes

Richard K. Gordon, *Member, IEEE*, and Raj Mittra, *Fellow, IEEE*

Abstract—A two-step technique for the analysis of axisymmetric radomes is presented in this paper. Initially, an axisymmetric finite element approach is employed, together with an absorbing boundary condition for mesh truncation, to determine the near fields scattered by an empty radome illuminated by a distant source. Next, the reciprocity theorem is invoked to determine the far-field pattern of an antenna encased by the radome, by computing the reaction between the current distribution on the antenna and the near-field data determined in the first step. The details of the formulation are presented along with numerical results for two different arrays enclosed by radomes of varying permittivities.

I. INTRODUCTION

THE problem of determining the modification of the radiation pattern of an antenna covered by a radome has been addressed recently by a number of researchers employing a variety of different approaches. Orta *et al.* [1] have used ray optical techniques in conjunction with the reciprocity theorem to address the radome problem, and a geometric theory of diffraction (GTD) approach has been employed by Chikaoka *et al.* [2] to solve the same. Arvas *et al.* [3] have presented a three-dimensional method of moments solution based on the use of the surface equivalence principle, whereas Robinson and his colleagues [4] have used a two-dimensional, oblique-incidence, method-of-moments solution to handle the problem. A two-dimensional finite element analysis that uses an absorbing boundary condition for mesh truncation has been employed by Povinelli and D'Angelo [5], and Chan and Mittra [6] have developed a spectral-domain approach for the analysis of a planar FSS radome.

In this paper, we present a general-purpose method for analyzing axisymmetric radomes with arbitrary inhomogeneities, which cannot be conveniently or accurately investigated by the ray optical techniques, the method of moments, or approximate two-dimensional approaches. We use the reciprocity theorem in conjunction with an axisymmetric finite element approach that employs a novel absorbing boundary condition for mesh truncation. We use a two-step procedure which initially employs the finite element method to determine the near fields within the radome when it is illuminated by a distant source. In the second step, the reciprocity theorem is used to find the far-field pattern of an antenna with a given current distribution located inside the radome, from the near-field information determined earlier in the first step. The method presented here assumes that the presence of the radome does not have a

significant effect on the antenna currents; it may not work if these currents are significantly changed by the presence of the radome.

II. FORMULATION

The details of the two-step procedure for radome analysis will now be described. To accomplish the first step, which consists of finding the near fields within the radome when it is illuminated by a distant source, we employ a finite element formulation based on the use of scaled versions of the coupled azimuthal potentials (CAP's) [7]. We now present a brief review of the approach used in the first step; for further details, the reader is referred to [8].

We begin by expressing E and H in terms of Fourier series expansions in ϕ as

$$E(\rho, \phi, z) = \sum_{m=-\infty}^{\infty} \begin{bmatrix} E_{\rho,m} \\ E_{\phi,m} \\ E_{z,m} \end{bmatrix} e^{jm\phi} \quad (1)$$

$$H(\rho, \phi, z) = \sum_{m=-\infty}^{\infty} \begin{bmatrix} H_{\rho,m} \\ H_{\phi,m} \\ H_{z,m} \end{bmatrix} e^{jm\phi} \quad (2)$$

The potentials we use in this problem are u_m and v_m , where

$$u_m = E_{\phi,m} \quad (3)$$

$$v_m = \eta_0 H_{\phi,m} \quad (4)$$

Inserting (3) and (4) into (1) and (2), and substituting the resulting equations into Maxwell's two curl equations, we obtain six scalar equations for each value of m . These six equations can be written as

$$E_{\rho,m} = j f_m \left(m \frac{\partial(\rho v_m)}{\partial \rho} + k_0 \rho^2 \mu_r \frac{\partial v_m}{\partial z} \right) \quad (5)$$

$$E_{z,m} = j f_m \left(m \rho \frac{\partial u_m}{\partial z} - k_0 \rho \mu_r \frac{\partial(\rho v_m)}{\partial \rho} \right) \quad (6)$$

$$H_{\rho,m} = j f_m \left(m \frac{\partial(\rho v_m)}{\partial \rho} - k_0 \rho^2 \epsilon_r \frac{\partial u_m}{\partial z} \right) \quad (7)$$

$$H_{z,m} = j f_m \left(m \rho \frac{\partial v_m}{\partial z} + k_0 \rho \epsilon_r \frac{\partial(\rho u_m)}{\partial \rho} \right) \quad (8)$$

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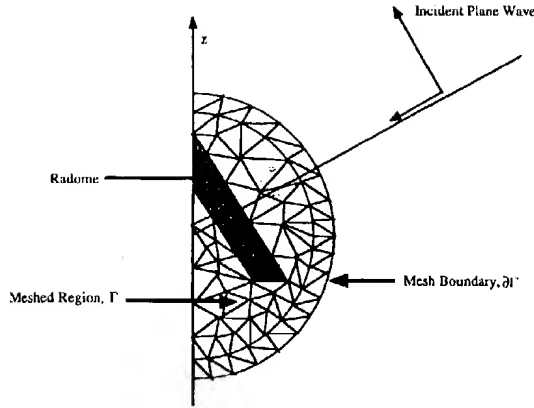


Fig. 1. Finite element mesh for analysis of axisymmetric radome.

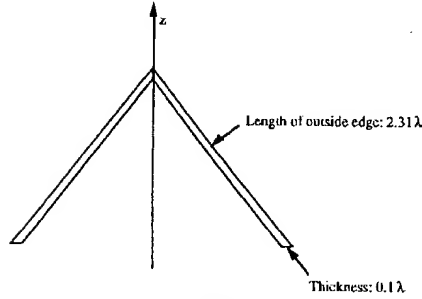


Fig. 2. Radome geometry.

$$u_m \epsilon_r + \nabla \cdot (f_m \rho \epsilon_r \nabla (\rho u_m)) + (m/k_0) \nabla \cdot (f_m \hat{\phi} \times \nabla (\rho v_m)) = 0 \quad (9)$$

$$v_m \mu_r + \nabla \cdot (f_m \rho \mu_r \nabla (\rho v_m)) - (m/k_0) \nabla \cdot (f_m \hat{\phi} \times \nabla (\rho u_m)) = 0, \quad (10)$$

where

$$f_m = (k_0^2 \mu_r(\rho, z) \epsilon_r(\rho, z) \rho^2 - m^2)^{-1}.$$

Equations (3)–(8) demonstrate that $E_{r,m}$, $E_{\phi,m}$, $E_{z,m}$, $H_{r,m}$, $H_{\phi,m}$, and $H_{z,m}$ can be expressed in terms of u_m and v_m . This implies that the BOR problem can be solved in terms of just the two unknowns, u_m and v_m , rather than all six components of \mathbf{E} and \mathbf{H} . Furthermore, because of the azimuthal symmetry of the body, rather than a three-dimensional mesh, this method requires only a two-dimensional mesh in any $\phi = \text{constant}$ plane, such as the one shown in Fig. 1. These two factors result in a significant reduction in the number of unknowns which, in turn, permits the analysis of significantly larger radomes.

Equations (9) and (10) describe the behavior of u_m and v_m in the meshed region. When each of these equations is multiplied by a testing function T , and then integrated over the entire meshed region Γ , the resulting equations can be

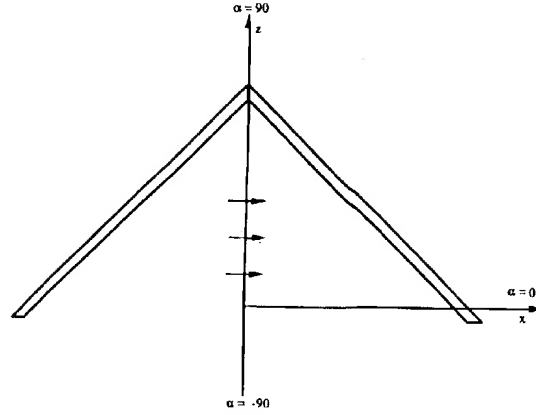


Fig. 3. Vertical array of dipoles.

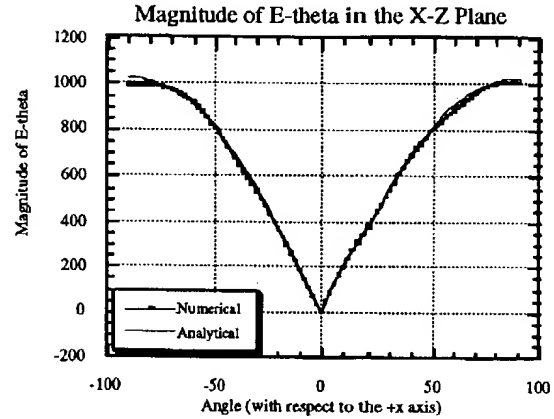


Fig. 4. Comparison of numerically and analytically determined patterns for transparent radome.

written, with the help of the divergence theorem, as

$$\begin{aligned} & \int_{\Gamma} T u_m \epsilon_r dA - \int_{\Gamma} f_m \rho \epsilon_r \nabla T \cdot \nabla (\rho u_m) dA \\ & - (m/k_0) \int_{\Gamma} f_m \nabla T \cdot (\hat{\phi} \times \nabla (\rho v_m)) dA \\ & = - \int_{\partial \Gamma} T f_m \rho \epsilon_r \frac{\partial (\rho u_m)}{\partial n} dl - (m/k_0) \\ & \cdot \int_{\partial \Gamma} f_m T (\hat{\phi} \times \nabla (\rho v_m)) \cdot \hat{n} dl \end{aligned} \quad (11)$$

$$\begin{aligned} & \int_{\Gamma} T v_m \mu_r dA - \int_{\Gamma} f_m \rho \mu_r \nabla T \cdot \nabla (\rho v_m) dA \\ & + (m/k_0) \int_{\Gamma} f_m \nabla T \cdot (\hat{\phi} \times \nabla (\rho u_m)) dA \\ & = - \int_{\partial \Gamma} T f_m \rho \mu_r \frac{\partial (\rho v_m)}{\partial n} dl + (m/k_0) \\ & \cdot \int_{\partial \Gamma} f_m T (\hat{\phi} \times \nabla (\rho u_m)) \cdot \hat{n} dl, \end{aligned} \quad (12)$$

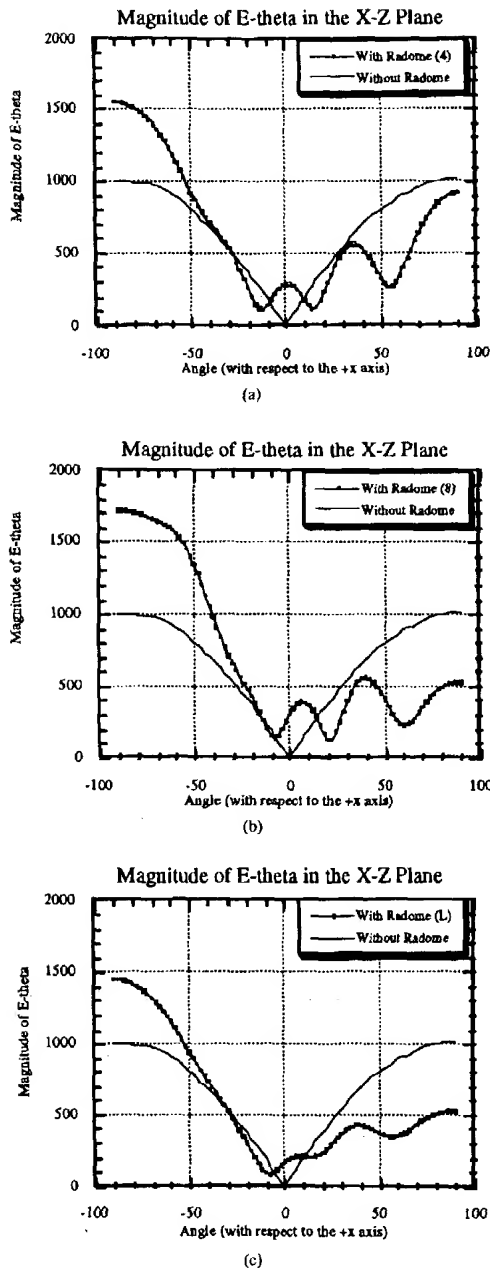


Fig. 5. Effect of radome on antenna pattern for $\epsilon_r =$ (a) 4.0, (b) 8.0, and (c) (4.0, -2.0).

where $\partial\Gamma$ is the boundary of the meshed region, Γ . These are the equations that are implemented using the finite element method. The first term on the right-hand side of each of these equations involves an integral of the normal derivative of an unknown along the outer boundary $\partial\Gamma$. These integrals

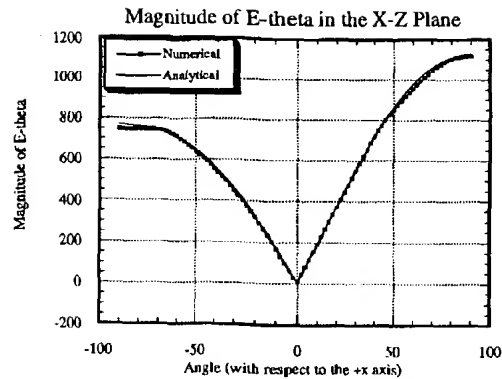


Fig. 6. Comparison of numerically and analytically determined patterns for transparent radome.

are evaluated with the assistance of an absorbing boundary condition derived from Wilcox's expansion for the scattered fields [9]. This technique is described in detail in [8].

The finite element solution for the near fields in the vicinity of the radome, when it is illuminated by a plane wave incident at some angle θ with respect to the z axis, completes the first step of the two-step procedure. Next, the reciprocity theorem is used to find the far field at the desired observation angle, for any antenna located anywhere within the radome. This is the second step of the two-step procedure, and is detailed below.

Let (J^a, M^a) and (J^b, M^b) be two sets of sources existing in the same linear medium and let E^a and H^a be the fields produced by (J^a, M^a) alone, and E^b and H^b be the corresponding fields produced by (J^b, M^b) alone. Then, by invoking the reciprocity theorem, we can show that

$$\iiint (E^a \cdot J^b - H^a \cdot M^b) d\tau = \iiint (E^b \cdot J^a - H^b \cdot M^a) d\tau. \quad (13)$$

Thus, for instance, if we set M^a and M^b to be zero, J^a to be the electric current distribution on the antenna, and J^b to be an electric dipole located far from the radome, then (13) can be used to determine the far-zone electric field, E^a , of the antenna radiating within the radome. In order to carry out this calculation, both J^a and E^b must be known. We assume that the presence of the radome has little effect on the antenna current distribution; consequently, J^a can be determined through an analysis of the antenna radiating in free space. We also note that E^b is the near electric field in the vicinity of the radome when it is illuminated by the electric dipole J^b . But this is precisely what we determined in the first step; that is, the plane wave that is used as the incident field in the first step is chosen to be the field that would be incident upon the radome if it were radiated by J^b . Thus, the electric field determined in the first step is identical to E^b . So, once the first step has been concluded for a particular location of J^b , (13) can be used to find, at this same location, the electric field radiated by the antenna within the radome. Similarly, the far magnetic field can be determined by setting J^b equal to

steps

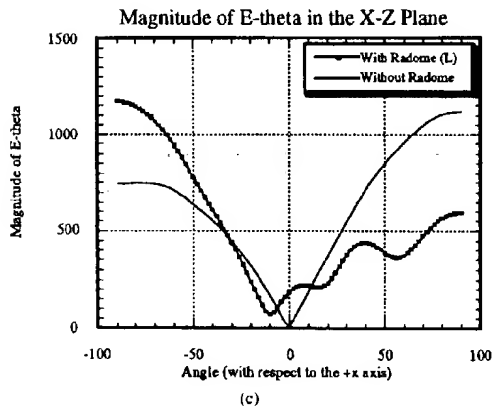
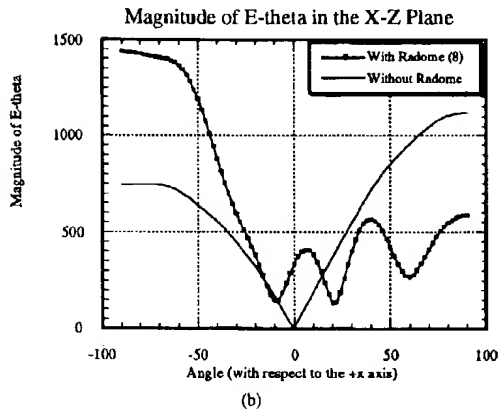
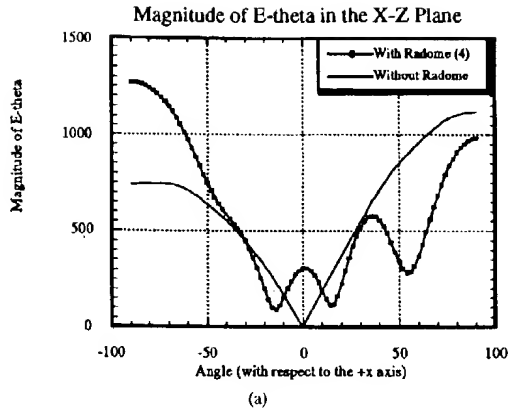


Fig. 7. Effect of radome on antenna pattern for $\epsilon_r =$ (a) 4.0, (b) 8.0, and (c) (4.0, -2.0).

zero and letting M^b be a magnetic dipole located far from the radome. We note at this point that it is unnecessary to recalculate the finite element matrix for each new location of J^b or M^b ; these sources affect only the incident field. Thus, the amount of computer time required to solve for 90 different source locations is only twice that required for a

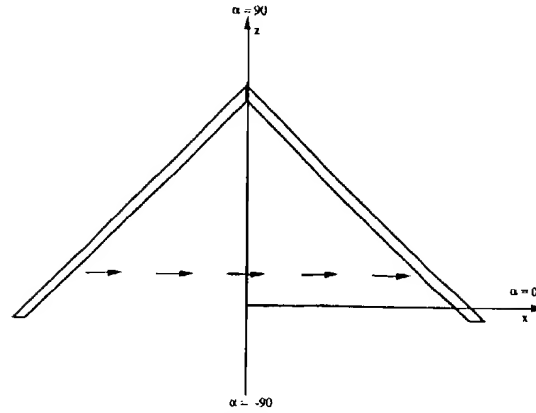


Fig. 8. Horizontal array of dipoles.

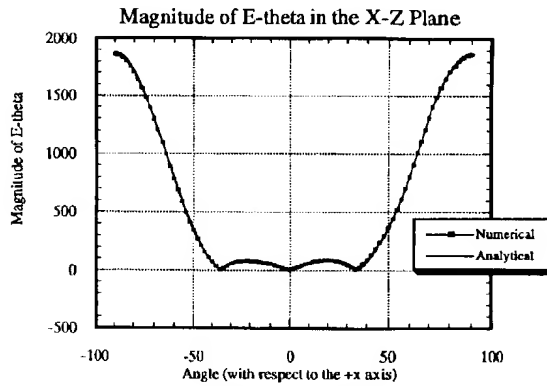


Fig. 9. Comparison of numerically and analytically determined patterns for transparent radome.

single location. Furthermore, we note that while the radome must have azimuthal symmetry, the antenna may have any shape and may be located anywhere within the radome. We now consider some numerical examples to demonstrate the use of this method.

III. NUMERICAL RESULTS

In this section we present some numerical results that illustrate the use of the method described above to analyze the radome geometry shown in Fig. 2. In each case, we consider a radome that has the shape of a truncated cone which is open at the bottom, although the method itself is general enough to handle any kind of closure of the radome, as long as the azimuthal symmetry is maintained. The length of the outside edge of the cone is $2.31\lambda_0$; its thickness is $0.1\lambda_0$. We will present the effects of varying the relative permittivity of the radome on the radiation patterns of two antenna arrays.

The first case we consider is shown in Fig. 3. The antenna is an array of three uniformly excited x -directed dipoles located on the z axis. The distance between consecutive dipoles is $0.0854\lambda_0$. We use the two-step procedure described above

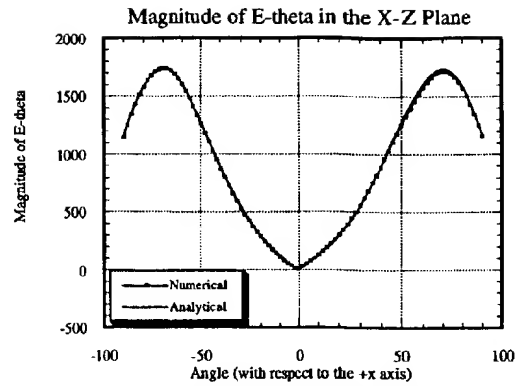
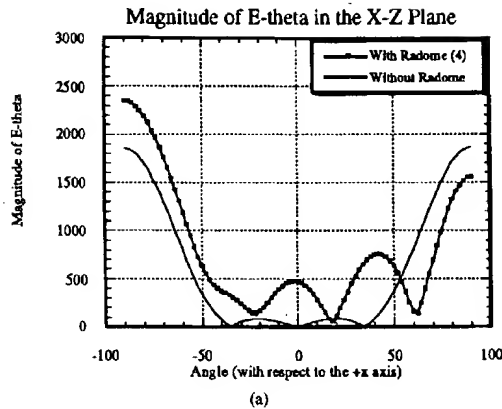


Fig. 11. Comparison of numerically and analytically determined patterns for transparent radome.

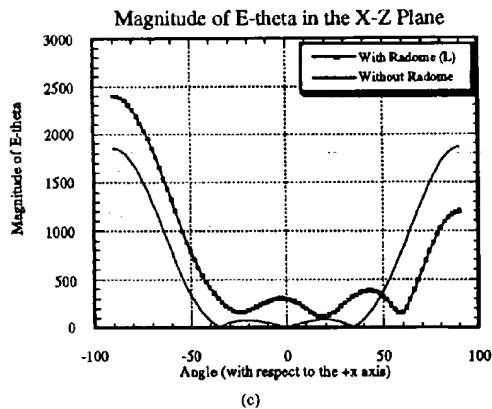
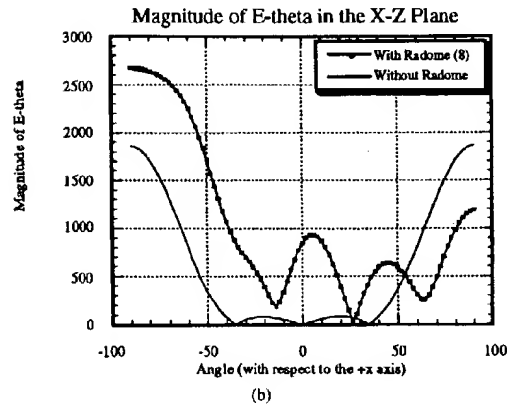


Fig. 10. Effect of radome on antenna pattern for $\epsilon_r =$ (a) 4.0, (b) 8.0, and (c) (4.0, -2.0).

to determine the far-field value of E_θ in the plane $\phi = 0^\circ$ for four different radome permittivities: $\epsilon_r = 1.0, 4.0, 8.0$, and (4.0, -2.0). The results for $\epsilon_r = 1.0$ are shown in Fig. 4. The reason we consider the case $\epsilon_r = 1.0$, i.e., the case of a transparent radome, is that for this problem an analytically determined pattern can be obtained for comparison

with the numerical results. As we can see from Fig. 4, in which the dotted line represents the numerical results while the solid line depicts the analytically determined pattern, the comparison is quite favorable. Note that this does not prove the validity of this technique but is a good check. In Fig. 5, we show the numerical results for $\epsilon_r =$ (a) 4.0, (b) 8.0, and (c) (4.0, -2.0). In each case, the dotted line represents the radiation pattern in the presence of the radome while the solid line depicts the pattern obtained in its absence. We note that, in each case, the null at 0° , i.e., in the positive x direction, has disappeared. The enhancement of the pattern near -90° can be attributed to the fact that the radome is open at the bottom. We also note the degradation of the pattern for most positive angles, i.e., looking through the radome.

In Figs. 6 and 7 we consider the same vertical array of three dipoles; but while the amplitude of the excitation for each dipole is still the same, a phase progression has now been introduced. The phase of the excitation on the bottom, middle, and top dipole, is $0.0^\circ, -27.86^\circ$, and -55.72° , respectively. Fig. 6 presents a comparison of the numerical and analytically determined results for the transparent radome, while Fig. 7 shows the effect on the radiation pattern of the presence of a radome of relative permittivity (a) 4.0, (b) 8.0, and (c) (4.0, -2.0). Like Fig. 4 above, Fig. 6 shows good agreement between the numerical results and the analytically determined pattern for the transparent radome. Fig. 7 shows the same general features that were observed in Fig. 5, but in this case the phase progression is present.

The second case we consider is shown in Fig. 8. The antenna is a horizontal array of five uniformly excited x -directed dipoles. The distance between consecutive dipoles is $0.247\lambda_0$. We again use the two-step procedure to determine the far-field value of E_θ in the plane $\phi = 0^\circ$ for four different radome permittivities: $\epsilon_r = 1.0, 4.0, 8.0$, and (4.0, -2.0). The results for $\epsilon_r = 1.0$ are shown in Fig. 9. Just as was the case for the vertical array, we see that there is good agreement between the numerical results and the analytically determined pattern for this horizontal array of uniformly excited dipoles. In Fig. 10 we see the numerical results for $\epsilon_r =$ (a) 4.0, (b) 8.0, and (c) (4.0, -2.0). We again note that as a result of the introduction

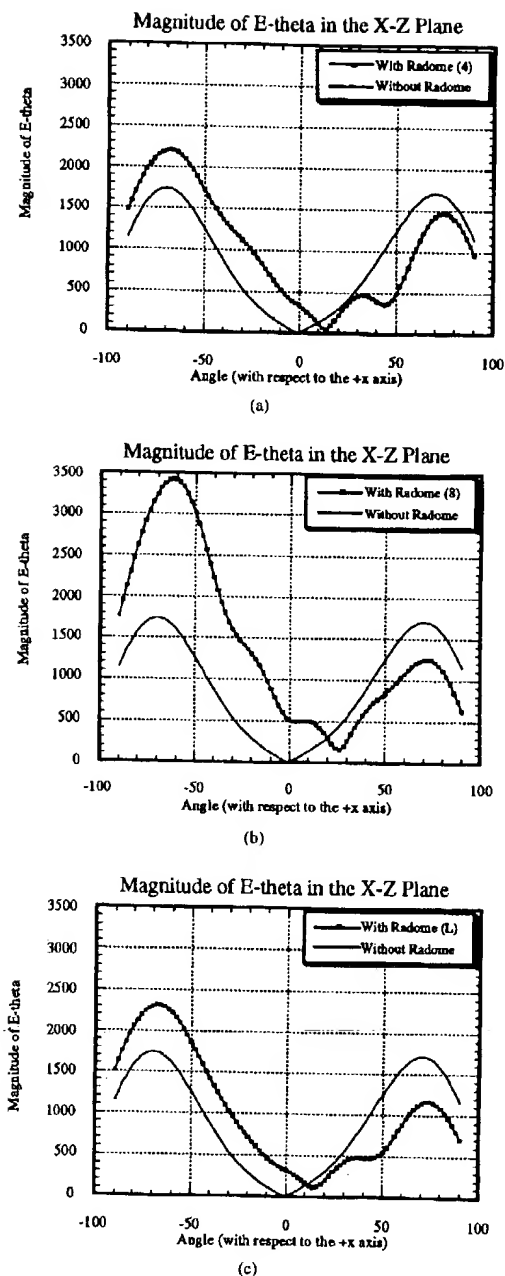


Fig. 12. Effect of radome on antenna pattern for $\epsilon_r =$ (a) 4.0, (b) 8.0, and (c) (4.0, -2.0).

of the radome, the null at 0° has disappeared, the pattern has been enhanced near -90° , and the pattern has been diminished at angles near $+90^\circ$.

The final results we present are for the same horizontal array of dipoles when the amplitude of the excitations is uniform but a phase progression is used. Proceeding from left to right, the

phases of the excitation on the first, second, third, fourth, and fifth dipoles are -75.16° , -37.58° , 0.0° , 37.58° , and 75.16° , respectively. Fig. 11 presents a comparison of the numerical and analytically determined results for the transparent radome, while Fig. 12 shows the effect on the radiation pattern of the presence of a radome of relative permittivity (a) 4.0, (b) 8.0, and (c) (4.0, -2.0). We again note, in Fig. 11, the good agreement between the numerical results and the analytically determined pattern for the transparent radome. Fig. 12 shows the expected effects of the presence of the radome on the antenna pattern.

IV. CONCLUSIONS

In this paper, we have considered a two-step technique for the analysis of inhomogeneous axisymmetric radomes. We have verified the approach by computing the radiation pattern of an unphased vertical array of dipoles, a phased vertical array of dipoles, an unphased horizontal array of dipoles, and a phased horizontal array of dipoles within a transparent radome for which the radiation pattern can be determined analytically. Next, we investigated the pattern of these same antennas covered by two lossless radomes and one lossy radome. By comparing the results for each case, it is possible to determine how the radiation pattern is affected by a change in the composition of the radome. Similarly, this method could also be used to determine the effect of changing the shape of the radome or the addition of a metallic tip.

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Coupled azimuthal potentials for electromagnetic fi problems in inhomogeneous axially symmetric med

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Abstract:

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Index Terms:

Electromagnetic scattering by nonhomogeneous media Loaded antennas Nonhomoge media Numerical methods

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Coupled Azimuthal Potentials for Electromagnetic Field Problems in Inhomogeneous Axially Symmetric Media

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Abstract—Classical electromagnetic potential formulations are, with the exceptions of a few special cases of one-dimensional stratification, restricted to use in uniform media. A recently developed potential formulation that provides a flexible basis for numerical computation of time-harmonic field problems involving continuously and discretely inhomogeneous axially symmetric media is the topic of this paper. The formulation manifests itself in both a differential equation system and, alternately, a variational criterion. Typical numerical applications include solutions of scattering by arbitrarily shaped material bodies of revolution and radiation from inhomogeneously loaded rotationally symmetric antenna structures. Current numerical investigations by the authors, using Mei's unimoment method in conjunction with both finite-difference and finite-element techniques, have shown the formulation to be highly feasible for computation of field problems having dimensions as large as several wavelengths.

I. INTRODUCTION

Numerical computation of time-harmonic electromagnetic boundary value problems has recently been extended into the regime of inhomogeneous axially symmetric media by way of the potential formulation to be presented in this paper. This formulation provides the basis for the numerical solution of an important class of interior, radiation, and scattering problems, involving inhomogeneous bodies of revolution having multiwavelength dimensions, which were heretofore unapproachable using conventional techniques.

Electromagnetic fields are traditionally represented in terms of potentials for ease of analysis. Potential formulations also offer numerical advantages by usually having fewer coupled unknowns and a higher order of continuity than the original electromagnetic field. Computation time is, in fact, proportional to the cube of the number of coupled scalar fields which are present as unknowns in the formulation. A general vector

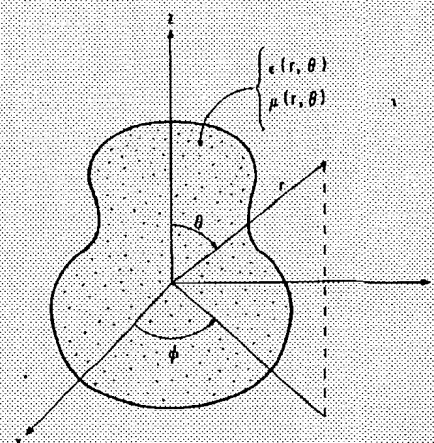


Fig. 1. Axially symmetric inhomogeneous medium.

potential representation may be developed for completely arbitrary inhomogeneous isotropic material, but the formulation is in terms of four coupled scalar fields [1]. Without potentials, Maxwell's equations must be solved using at least three coupled scalar functions: namely the vector of either the electric or the magnetic field, which are in general discontinuous at material interfaces. Classical TE and TM potential formulations generate all fields from only two uncoupled scalar functions, but are only valid for uniform media and some special cases of separable coordinate one-dimensional inhomogeneities, such as that of a spherically stratified media [1], [2].

The potential formulation to be presented here is valid in generally inhomogeneous isotropic rotationally symmetric media, as shown in Fig. 1, where the constitutive parameters $\epsilon(r)$ and $\mu(r)$ are invariant to the azimuthal coordinate ϕ . All electromagnetic field components are expanded via exponential Fourier series in the ϕ -coordinate. The modal electromagnetic fields are shown to be representable by two coupled azimuthal potentials (CAP's), so named because of their one-to-one relationship with the azimuthal components of the modal electric and magnetic fields. The potentials in the CAP formulation, which are everywhere continuous, are then shown to satisfy a system of coupled partial differential equations and, alternately, a variational criterion, either of which can be used as a basis for developing numerical solution algorithms.

The range of possible application of this new potential representation of Maxwell's equations includes the numerical solutions of both interior region Dirichlet type problems and open region radiation and scattering problems, using Mei's "unimoment method" [3]. The CAP formulation can be readily employed, in conjunction with appropriate numerical techniques, to solve such typical problems as scattering by distorted raindrops, power absorption by azimuthally invariant biological tissue models, and effects of inhomogeneous dielectric loading on axially symmetric antenna structures and waveguide sections.

II. MODAL FIELD DECOMPOSITION AND GENERATING EQUATIONS

The normalized coordinates to be used in the subsequent equations are defined by $(R, Z, \phi) = (k_0 \rho, k_0 z, \phi)$, where (ρ, z, ϕ) are standard circular cylindrical coordinates and $k_0 = 2\pi/\lambda_0$ is the free-space wavenumber of the time-harmonic

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field. The reason for this particular choice of coordinates is twofold. First, the use of this normalized coordinate system yields very compact equation presentations, and second, these coordinates form a two-dimensional Cartesian system in the spatial solution domain for the CAP formulation. This latter property is of particular value for use with the finite-element method, where numerical surface integrations must be performed over the two-dimensional spatial solution domain. The relative constitutive parameters of the medium, $\epsilon_r(R, Z)$ and $\mu_r(R, Z)$, are invariant to the ϕ -coordinate.

The equations of the CAP formulation are obtained by first decomposing the total fields into azimuthal modes via an exponential Fourier series in the ϕ -coordinate

$$\bar{E}(R, Z, \phi) = \sum_{m=-\infty}^{\infty} \bar{e}_m(R, Z) \exp(jm\phi) \quad (1a)$$

$$\eta_0 \bar{H}(R, Z, \phi) = \sum_{m=-\infty}^{\infty} \bar{h}_m(R, Z) \exp(jm\phi) \quad (1b)$$

where $\eta_0 = 120\pi \Omega$. Due to the assumed axial symmetry of the medium, the modal fields have time-average power orthogonality and decouple when the field expansions in (1) are substituted into Maxwell's time-harmonic source-free equations, yielding the first-order coupled system given by

$$\epsilon_r e_{\phi,m} = j \left[\frac{\partial h_{Z,m}}{\partial R} - \frac{\partial h_{R,m}}{\partial Z} \right] \quad (2a)$$

$$\mu_r h_{\phi,m} = j \left[\frac{\partial e_{R,m}}{\partial Z} - \frac{\partial e_{Z,m}}{\partial R} \right] \quad (2b)$$

$$R \epsilon_r e_{R,m} = j \left[\frac{\partial(R h_{\phi,m})}{\partial Z} - j m h_{Z,m} \right] \quad (2c)$$

$$R \mu_r h_{R,m} = j \left[j m e_{Z,m} - \frac{\partial(R e_{\phi,m})}{\partial Z} \right] \quad (2d)$$

$$R \epsilon_r e_{Z,m} = j \left[j m h_{R,m} - \frac{\partial(R h_{\phi,m})}{\partial R} \right] \quad (2e)$$

$$R \mu_r h_{Z,m} = j \left[\frac{\partial(R e_{\phi,m})}{\partial R} - j m e_{R,m} \right] \quad (2f)$$

where the azimuthal dependence of the modal fields is suppressed. Using judicious substitution between (2c) and (2f), and between (2d) and (2e), it is easily found that all modal field components can be generated from two modal scalar potential functions $\psi_1(R, Z, m)$ and $\psi_2(R, Z, m)$, via

$$\hat{\phi} \times \bar{e}_m = j f_m (m \hat{\phi} \times \nabla \psi_1 - R \mu_r \nabla \psi_2) \quad (3a)$$

$$\hat{\phi} \cdot \bar{e}_m = \psi_1 / R \quad (3b)$$

$$\hat{\phi} \times \bar{h}_m = j f_m (m \hat{\phi} \times \nabla \psi_2 + R \epsilon_r \nabla \psi_1) \quad (3c)$$

$$\hat{\phi} \cdot \bar{h}_m = \psi_2 / R \quad (3d)$$

where $\hat{\phi}$ is the unit azimuthal vector, the two-dimensional gradient operator is defined by

$$\nabla = \hat{R} \frac{\partial}{\partial R} + \hat{Z} \frac{\partial}{\partial Z} \quad (4a)$$

and

$$f_m(R, Z) = [\mu_r(R, Z) \epsilon_r(R, Z) R^2 - m^2]^{-1}. \quad (4b)$$

As was previously mentioned, the normalized cylindrical coordinates (R, Z, ϕ) were chosen only for the practical reasons of compact presentation and utility in finite-element numerical computations. The equations of the CAP formulation can be easily obtained in an arbitrary coordinate system (u_1, u_2, ϕ) , where u_1 and u_2 are both orthogonal to ϕ and form some single-valued system of coordinates in any constant azimuth planar cross section of the region of revolution. For example, the equations throughout this paper can be trivially recast into standard spherical coordinates (r, θ, ϕ) using the simple substitutions $R = k_0 r \sin \theta$, $Z = k_0 r \cos \theta$, and $\nabla = [(1/k_0) \hat{r}(\partial/\partial r) + \hat{\theta}(1/r)(\partial/\partial \theta)]$.

A very important property of the potentials can be obtained easily by noting that since the modal potentials are proportional to the ϕ -components of \bar{e}_m and \bar{h}_m , as shown in (3b) and (3d), they are continuous everywhere, including at dielectric and magnetic interfaces. This property of uniform field continuity is very desirable in numerical computations. For the case of the variational finite-element method the utility of the potential field continuity is particularly pronounced, in that material interfaces require no supplemental boundary conditions and are handled naturally with the same general algorithm as is continuously inhomogeneous media.

III. DIFFERENTIAL EQUATION REPRESENTATION

The partial differential equations obeyed by the coupled azimuthal potentials ψ_1 and ψ_2 may be obtained directly from Maxwell's equations by substitution of the modal field generating equations in (3) into (2a) and (2b). The potentials are found to satisfy a system of coupled second-order linear partial differential equations given by

$$\nabla \cdot [f_m(R \epsilon_r \nabla \psi_1 + m \hat{\phi} \times \nabla \psi_2)] + \epsilon_r \psi_1 / R = 0 \quad (5a)$$

$$\nabla \cdot [f_m(R \mu_r \nabla \psi_2 - m \hat{\phi} \times \nabla \psi_1)] + \mu_r \psi_2 / R = 0 \quad (5b)$$

where the gradient operator ∇ is as defined previously in (4a) and $f_m(R, Z)$ is given by (4b).

To utilize the unimoment technique in obtaining solutions to open region radiation and scattering problems requires the ability to solve interior Dirichlet type boundary value problems within a closed region containing the inhomogeneities of the problem, (e.g., an antenna structure or scattering bodies). In solving such an interior Dirichlet problem the two-dimensional solution domain of (5) is a planar constant- ϕ cross section of an interior volume of revolution, as is illustrated in Fig. 2. The interior region S , which is bounded by the curve C , contains inhomogeneous material specified by the relative constitutive parameters $\epsilon_r(R, Z)$ and $\mu_r(R, Z)$. The surface S could, for example, be the semicircular cross section of a geometrical sphere which contains an arbitrarily shaped, (and possibly inhomogeneous), material body of revolution, such as a torus.

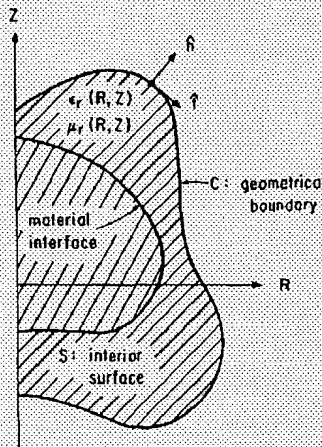


Fig. 2. Constant azimuth planar cross section.

The question of uniqueness of the solution to the coupled system in (5), for arbitrary Dirichlet boundary conditions of the potentials specified on C , may be resolved by using the standard proof for electromagnetic field uniqueness assuming nonzero losses [4], where it is noted that ψ_1 and ψ_2 are proportional to the ϕ -components of \vec{e}_m and \vec{h}_m , respectively.

For the special case of azimuthally invariant modal fields ($m = 0$), the differential equations in (5) decouple, giving a simple potential formulation that was originally derived by Abraham and is given more currently by Stratton [5]. This uncoupled formulation was the basis for a recently completed investigation of inhomogeneous dielectric loading of biconical antenna structures, conducted by Stovall and Mei, using finite-difference simulation of the PDE for ψ_2 when $m = 0$ [6]. It should be noted that only for the case of the axially symmetric mode ($m = 0$), can the total modal field be decomposed into partial fields which are either TE or TM to $\hat{\phi}$. This constraint expresses the fact that no azimuthally changing modal electromagnetic field ($m \neq 0$) can be generated having a null azimuthal component of either \vec{e}_m or \vec{h}_m throughout an axially symmetric source-free volume of revolution. This result is valid even when ϵ and μ are constant, which is perhaps the reason why the CAP formulation has been overlooked by classical electromagnetic analysts.

To further investigate the nature of the system of CAP PDE's in (5) we will use matrix operator notation to recast the equations into a more compact form. Defining the solution vector

$$\psi(R, Z, m) = \begin{bmatrix} \psi_1(R, Z, m) \\ \psi_2(R, Z, m) \end{bmatrix} \quad (6)$$

and the matrix differential operator

$$A(R, Z, m) = \begin{bmatrix} \nabla \cdot (f_m R \epsilon_r \nabla) + \epsilon_r / R & m \nabla \cdot (f_m \hat{\phi} \times \nabla) \\ -m \nabla \cdot (f_m \hat{\phi} \times \nabla) & \nabla \cdot (f_m R \mu_r \nabla) + \mu_r / R \end{bmatrix} \quad (7)$$

the system in (5) is given by

$$A\psi = 0 \quad (8a)$$

with Dirichlet BC's on C given by

$$\psi(R, Z, m)|_C = \beta(c). \quad (8b)$$

A very important property of the operator A is its formal self-adjointness on the space of vector functions having homogeneous Dirichlet BC's on C .

$$\langle u, Av \rangle = \langle v, Au \rangle \quad (9)$$

where the nonconjugated inner dot product is defined by

$$\langle a, b \rangle = \int_S a(R, Z) \cdot b(R, Z) dR dZ \quad (10)$$

and the vector functions in (9) satisfy the adjoint boundary condition $u|_C = v|_C = 0$. As a consequence of this operator self-adjointness it follows directly that a variational principle exists for the CAP formulation.

IV. VARIATIONAL FORMULATION

The numerical solution of the system of PDE's in (5) via finite-difference simulation requires the use of basis functions which are twice differentiable. This continuity constraint on the basis functions may be relaxed to only first-order differentiability if a variational formulation is used in conjunction with the finite-element method.

In establishing a variational principle we will follow two separate, but equivalent, routes. Our first avenue is the Euler-Lagrange formulation which provides the simplest, but somewhat indirect, approach to a variational criterion. The second development relies upon the self-adjointness of the system operator A in conjunction with the application of a stationary theorem, to provide direct access to a variational principle.

The Euler-Lagrange variational formulation is based upon the existence of a functional of the potentials and their first derivatives which is stationary about the correct solution of (5) for given Dirichlet BC's on the boundary curve C of Fig. 2. The functional manifests itself as a surface integral over the planar cross section surface S ,

$$F = \int_S L(R, Z, \psi_1, \psi_2, \nabla\psi_1, \nabla\psi_2) dR dZ \quad (11)$$

It is well known from the calculus of variations that at the stationary point of the functional F the Lagrangian L satisfies a system of coupled Euler-Lagrange partial differential equations [7],

$$\nabla \cdot \left[\frac{\partial L}{\partial (D_R \psi_k)} \hat{R} + \frac{\partial L}{\partial (D_Z \psi_k)} \hat{Z} \right] - \frac{\partial L}{\partial \psi_k} = 0, \quad k = 1, 2. \quad (12)$$

The foremost problem in deriving such a variational criterion, using an original differential equation formulation, is to discover the Lagrangian L which when substituted into (12) will yield the original system of PDE's. This unearthing of the Lagrangian is not always a simple matter, particularly in cases of greater than second-order PDE's where higher order derivative terms appear in the Lagrangian and the Euler-Lagrange system is more complicated than in (12).

The discovery of the Lagrangian for the CAP formulation is most quickly performed by a detailed inspection process, which yields,

$$L = f_m [\nabla\psi_1 \cdot (R\epsilon_r \nabla\psi_1 + m\hat{\phi} \times \nabla\psi_2) + \nabla\psi_2 \cdot (R\mu_r \nabla\psi_2 - m\hat{\phi} \times \nabla\psi_1)] - (\epsilon_r \psi_1^2 + \mu_r \psi_2^2) / R. \quad (13)$$

This result, which is unique to within an arbitrary constant multiplier and independent additive function, may be verified by direct substitution into (12).

The second approach to establishing a variational principle is via a "stationary theorem" applicable to formally self-adjoint operators [8]. This stationary theorem is directly extendable to the matrix operator equation of (8). In particular, because of the self-adjoint nature of A , if we have a boundary value problem of the type,

$$A\Psi = \Phi \quad (14a)$$

with homogeneous Dirichlet BC's

$$\Psi(R, Z, m)|_C = 0 \quad (14b)$$

where $\Phi(R, Z, m)$ is some known driving vector, then a functional that is stationary about the correct solution of (14) is given by

$$G = 2\langle \Psi, \Phi \rangle - \langle \Psi, A\Psi \rangle \quad (15)$$

where the inner products are defined in (10).

The conversion of the CAP system in (8) to one of the form in (14) is accomplished by the simple change of variables,

$$\Psi(R, Z, m) = \psi(R, Z, m) - \beta(R, Z) \quad (16a)$$

$$\Phi(R, Z, m) = -A\beta(R, Z) \quad (16b)$$

where $\beta(R, Z)$ is any arbitrary vector function satisfying the same boundary conditions on C as does $\psi(R, Z, m)$. Substituting (16) into (15) yields

$$G = -\langle \psi, A\psi \rangle - \langle \psi, A\beta \rangle + \langle \beta, A\psi \rangle + \langle \beta, A\beta \rangle. \quad (17)$$

Using direct vector calculus operations on the combination of the second and third inner products, which is commonly referred to as the bilinear concomitant of ψ and β , it will be found that G can be written as

$$\begin{aligned} G = & \{ -\langle \psi, A\psi \rangle + \oint_C \psi_1 f_m (R\epsilon_r \nabla \psi_1 + m\hat{\phi} \times \nabla \psi_2) \\ & + \psi_2 f_m (R\mu_r \nabla \psi_2 - m\hat{\phi} \times \nabla \psi_1) \cdot \hat{n} | dC \} \\ & - \left\{ -\langle \beta, A\beta \rangle + \oint_C \beta_1 f_m (R\epsilon_r \nabla \beta_1 + m\hat{\phi} \times \nabla \beta_2) \right. \\ & \left. + \beta_2 f_m (R\mu_r \nabla \beta_2 - m\hat{\phi} \times \nabla \beta_1) \cdot \hat{n} | dC \right\}. \quad (18) \end{aligned}$$

This can be recast into a more compact form by noting that the terms within each set of curly brackets can be recombined to yield a surface integral of the exact form of the Euler-Lagrange functional in (11) and (13). The result is

$$\begin{aligned} G = & \int_S L(R, Z, \psi_1, \psi_2, \nabla \psi_1, \nabla \psi_2) dR dZ \\ & - \int_S L(R, Z, \beta_1, \beta_2, \nabla \beta_1, \nabla \beta_2) dR dZ = F_\psi - F_\beta. \quad (19) \end{aligned}$$

The stationary functionals G and F , as given in (17) and (11), respectively, thus differ only by a functional of the arbitrary and independent vector β and its derivatives: namely F_β , whose first variation with respect to the solution vector ψ is zero. The Euler-Lagrange and stationary theorem approaches thus yield stationary functionals which are precisely equivalent in the variational sense.

In numerical applications of this variational criterion, using the finite-element method, it is often convenient to change variables and select as the fundamental unknowns the ϕ -components of the modal fields, $e_{\phi,m}(R, Z) = \psi_1/R$ and $h_{\phi,m}(R, Z) = \psi_2/R$. If linear basis functions are used to approximate the potentials ψ_1 and ψ_2 then the last quadratic term in the Lagrangian in (8), $(\epsilon_r \psi_1^2 + \mu_r \psi_2^2)/R$, will introduce a nonintegrable infinite singularity along the Z axis, where $R = 0$. The change of variables previously mentioned eliminates this singularity effect, but it then becomes necessary to know the boundary conditions obeyed by $e_{\phi,m}$ and $h_{\phi,m}$ along the section(s) of the Z axis which bound the surface S . These boundary conditions can be obtained via a judicious cross substitution and limiting procedure using Maxwell's equations, and are given here for reference purposes:

$$e_{\phi,m}(R, Z)|_{R=0} = h_{\phi,m}(R, Z)|_{R=0} = 0, \text{ for } m^2 \neq 1 \quad (20a)$$

$$3 \frac{\partial h_{\phi,m}}{\partial R} + \left(\frac{\partial \ln \epsilon_r}{\partial R} \right) e_{\phi,m} \Big|_{R=0} = 0, \text{ for } m^2 = 1 \quad (20b)$$

$$3 \frac{\partial h_{\phi,m}}{\partial R} + \left(\frac{\partial \ln \mu_r}{\partial R} \right) h_{\phi,m} \Big|_{R=0} = 0, \text{ for } m^2 = 1. \quad (20c)$$

The homogeneous Dirichlet BC's for $m^2 \neq 1$, in (20a), appear as an obvious result of the continuity and single-valuedness of the vector EM field as the Z axis is approached from all constant azimuth paths. The Cauchy BC's for the case of $m^2 = 1$, in (20b) and (20c), reduce to homogeneous Neumann BC's, (radial derivatives equal to zero), for the case of media composed of uniform material bodies of revolution.

A final important topic associated with the variational formulation concerns the physical interpretation of the stationary functional F , as displayed in (11) and (13). Using simple substitutions from (3), it can be shown that the Lagrangian in (13) can be written in terms of the modal vector electromagnetic field as

$$L = -R(e_r \bar{e}_m \cdot \bar{e}_m + \mu_r \bar{h}_m \cdot \bar{h}_m) - 2m\hat{\phi} \cdot (\bar{e}_m \times \bar{h}_m). \quad (21)$$

A direct vector manipulation of Maxwell's curl equations for the modal fields will show that this can be alternately written as

$$L = -jR \nabla' \cdot [(I - \hat{\phi}\hat{\phi}) \cdot (\bar{e}_m \times \bar{h}_m)] \quad (22)$$

where I is the identity dyadic and ∇' is the conventional three-dimensional divergence operating on the transverse (to $\hat{\phi}$) vector components of the "pseudo" Poynting vector, $\bar{e}_m \times \bar{h}_m$. Upon substituting (22) into (13), the divergence theorem can be used to transform the surface integral of F into a line integral around C of the outward normal of the "pseudo" Poynting vector:

$$F = -j \oint_C (\bar{e}_m \times \bar{h}_m) \cdot \hat{n} | dC |. \quad (23)$$

The term "pseudo" is used because no conjugates appear in the cross products in the integrand, as would be the case if the terms were related to time-average power. The physical significance of the stationary functional F can be displayed by considering the time-varying power per unit azimuth radian of the m th order modal field that is radiated outward from a constant- ϕ planar cross section. This time-varying power density can be written as

$$\frac{\partial P(\phi, t)}{\partial \phi} = \frac{1}{2\eta_0 k_0^3} \operatorname{Re} \left\{ \oint_C (\bar{e}_m \times \bar{h}_m^*) \cdot \hat{n} R |dc| + \left[\oint_C (\bar{e}_m \times \bar{h}_m) \cdot \hat{n} R |dc| \right] e^{j2(\omega t + m\phi)} \right\} \quad (24)$$

where the integral containing the magnetic field conjugate \bar{h}_m^* represents time-average power while the term in square brackets is the stationary functional F . The functional F is clearly associated with the difference of the time-varying and time-average radiated power densities. The exact physical interpretation of the stationarity of F appears somewhat illusive and the quest for such an interpretation certainly warrants further consideration.

V. CONCLUSION

The CAP formulation provides an important foundation for performing efficient numerical computations of solutions to the often encountered class of field problems involving axially symmetric media. Using the unimoment method, scattering and radiation problems can be handled very effectively by coupling exterior radiation field series solutions to interior region Dirichlet boundary value problems, which are solved either through finite-difference simulation of the CAP differential equation system [8], or through use of the variational finite-element technique.

In addition to the CAP formulation there have been discovered two alternate coupled scalar potential representations that utilize as potentials either the two vector components of $\hat{\phi} \times \bar{e}_m$ or the components of $\hat{\phi} \times \bar{h}_m$. There is, however, apparently no Euler-Lagrange functional for these formulations.

The authors currently have a very successful and operational numerical code which solves for EM scattering by arbitrarily shaped, and generally lossy, dielectric and magnetic bodies of revolution using the variational finite-element method. A detailed description of the implementation of this numerical method, along with extensive experimental and analytical verification, will be the topic of a forthcoming paper.

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Some Extensions of Babinet's Principle in Electromagnetic Theory

THOMAS B. A. SENIOR, FELLOW, IEEE

Abstract—The concept of resistive and conductive sheets provides a meaningful extension of Babinet's principle to surfaces which are no longer perfect. The complementary problems are described, and the appropriate field relations derived.

Babinet arrived at the principle, which now bears his name, by comparing the diffraction pattern of an aperture with that of a complementary disk. It was later verified for scalar waves subject to a Neumann or Dirichlet boundary condition on the screen or disk, and extended to electromagnetic waves by Booker [1] who pointed out the polarization rotation of the primary field which is necessary if the screen and disk are both perfectly conducting.

These known forms of Babinet's principle are all consequences of the symmetry of the fields radiated by planar distributions and (where appropriate) the duality of electromagnetic fields. Over the years there have been a number of attempts to extend the principle to surfaces which are not perfect, for example, by Neugebauer [2] to surfaces which are absorbing, and more recently by Lang [3] to resistive surfaces. In Lang's extension the complementary structures are a perfectly conducting screen with a resistive insert and a resistive screen with a perfectly conducting insert, but the derivation has been criticized [4] for the assumptions made concerning the normal components of the field. Nevertheless, as noted by Baum and Singaraju [5], resistive sheets and their electromagnetic duals do afford an exact extension of Babinet's principle. This fact was exploited by Senior [6] in developing some generalized forms in acoustics, and we here discuss the analogous results for electromagnetic waves.

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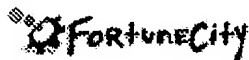
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Jets-In-Crossflow Mixing

Clifford E. Smith, Principal Investigator

Co-investigators: Daniel B. Bain and James D. Holdeman

CFD Research Corporation/NASA Lewis Research Center

Research Objective

The objectives of this work were to identify improved mixing schemes for rich-burn/quick-mix/lean-burn combustors applicable to advanced aircraft engines and to assess the effects of design parameters on mixing effectiveness. Efforts were focused on jet mixing in rectangular cross-sectional geometries.

Approach

Numerical parametric studies were performed on different orifice configurations. The computational analyses were performed using a three-dimensional Navier-Stokes flow solver (CFD-ACE) capable of analyzing turbulent reacting flows in complex geometries. The numerical results were examined using an interactive visualization package (CFD-VIEW).

Accomplishment Description

Over 60 orifice configurations were analyzed and assessed. The modeled geometry consisted of a rectangular duct with a row of jets on the top and bottom walls. Isothermal flow conditions were assumed. Systematic, parametric analyses were performed, consisting of variations in (1) orifice lateral alignment (in-line and staggered), (2) jet-to-mainstream (J) momentum flux ratio (16, 36, 64), (3) orifice aspect ratio (4:1, 2:1, 1:1, circle), (4) jet-to-mainstream mass flow (MR) ratio (2.0, 0.50, 0.25), and (5) orifice spacing-to-duct height (S/H) ratio ($0.125 \leq S/H \leq 1.5$). The numerical calculations were performed with grids varying in size from 50,000-150,000 cells that required approximately 2-4 Cray Y-MP hours and 10-15 megawords of memory.

Significance

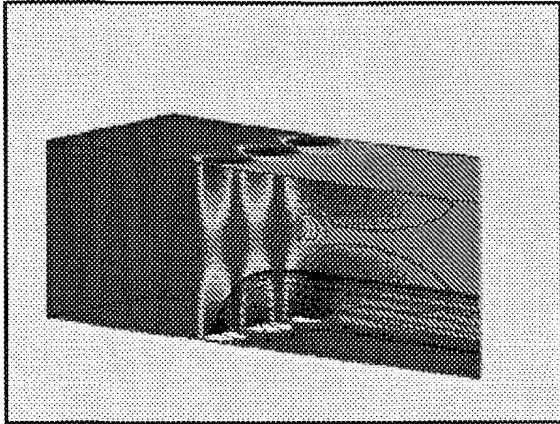
At optimum S/H, in-line lateral arrangements produced faster initial mixing than non-impinging, staggered arrangements due to their smaller geometric orifice size. Previous publications show that $S/H ((\text{root}) J)$ is a practical design parameter for mixing optimization even at high MR, and increasing J improves initial mixing at optimum S/H.

Future Plans

The effect of mass flow ratio and aspect ratio on mixing effectiveness will be assessed, and emission characteristics will be inferred from existing cold-flow data.

Publication

Bain, D. B.; Smith, C. E.; and Holdeman, J. D.: CFD Mixing Analysis of Axially Opposed Rows of Jets Injected Into Confined Crossflow. AIAA Paper 93-2044, June 1993.



Typical jet mixing numerical results. In-line circular orifices: $S/H = 0.375$, $J = 36$, $MR = 2.0$. Jet mass fraction: red = 0.0 to blue = 1.0.

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